

# The Value of a Measurement is in the Application of its Result

## Applied Metrology 101

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# Metrology

**Metrology** (met´ rol u jee) n. 1 The science or study of measurement.

**Applied Metrology:**

*Making measurement useful.*

# Applied Metrology 101

- The pursuit of knowledge.
  - The goal.
- Question everything.
  - The measurand.
- The investigation.
  - The measurement
- The implications.
  - The application and uncertainty.

# The Pursuit of Knowledge

"To measure is to know."

*- Lord Kelvin (1824-1907)*

First and Foremost:

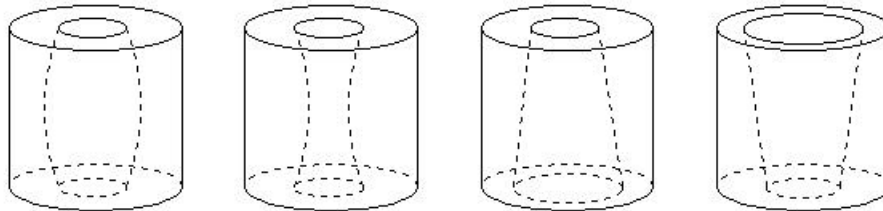
What is your reason for measuring?

# Question Everything

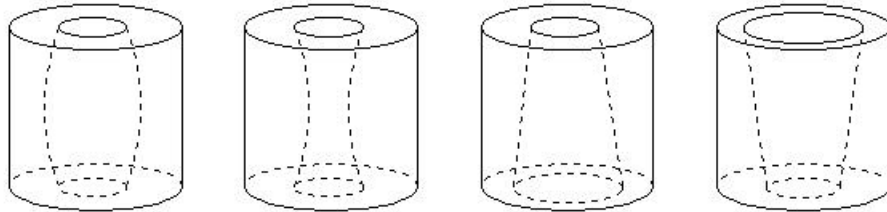
- What do you want to know about your process or product?
- Defining the measurand:
  - Be specific.
  - Do you require an answer that is numerical, graphical or both?
  - To what degree do you need to know this?
    - Be practical here, there are tradeoffs!!!

# The Measurand

- Be specific
  - The better that you can define a functional measurand the more useful the results will be.
  - Example:
    - Honing Stroke adjustment.

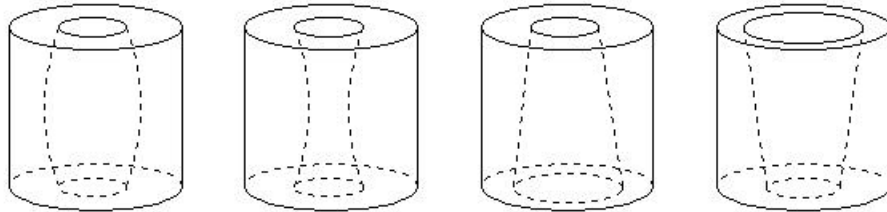


# The Measurand



- This isn't necessarily "Cylindricity"!!!
  - Cylindricity also incorporates "Roundness" and "Centerline Deviations".
  - This is a linear/parabolic variation in diameter!!!

# The Measurand



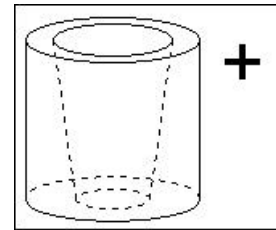
- Be very careful concerning language!
  - Often, instrument manufacturers will define their own terms:
    - Parallelism
    - Taper
    - Diameter Variation



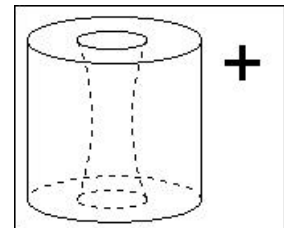
# The Measurand

- Given a very specific definition (and defined conventions) a numerical results may be adequate.

- Positive/Negative Taper
  - Based on linear regression



- Positive Negative Hourglass
  - Based on parabolic regression



# The Investigation

- Upon defining the measurand, we need to select the right equipment and make the measurement.

- This is analogous to the detective pulling out his kit and dusting for fingerprints.

“Surface finish is the fingerprint of the manufacturing process”

– *David Whitehouse*

# The Measurement

- At some point you are going to have to make the commitment and acquire a result.
  - Up to this point, things have been rather theoretical.
- Measurement is based on a system or process, not just a gage.
  - The result is from the system!!!

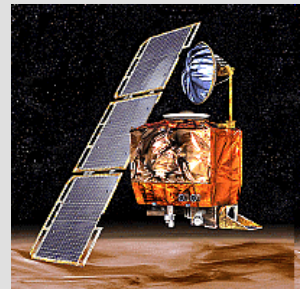
# The Measurement

- The Measurement System
  - Gage (and the condition thereof)
    - Attributes: tip radius, data points, math, etc.
  - Calibration/Traceability (or the lack thereof)
  - Operator (skill level)
  - Procedures (and the following thereof)
  - Environment
    - Temperature, cleanliness, vibration, etc.
  - Workpiece
    - Temperature, Cleanliness, fixturing, etc.

# The Measurement

- The measurement system provides some numerical/graphical result.
  - Does the result have the necessary “traceability” information
    - **Operator, Date, Time, Calibration Info, units, Part/Serial Numbers, etc.**
    - Results should be able to “Stand Alone”.
    - Does the Mars Climate Orbiter ring any bells!?!?
    - This isn’t rocket science!

R.I.P.

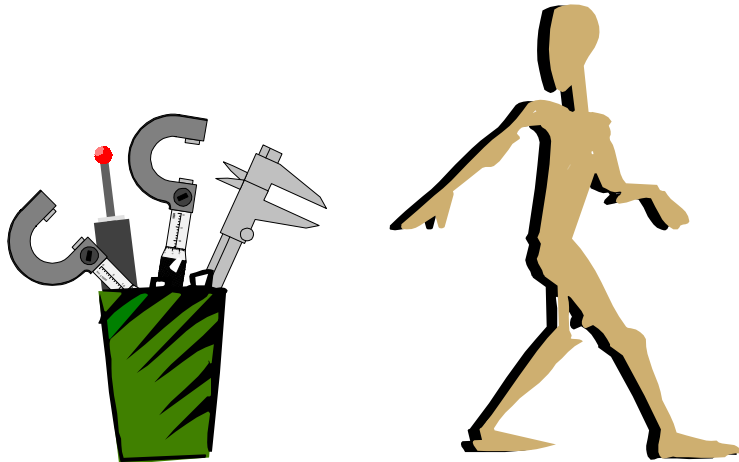


# The Implications

- Commonly heard:

*“If the results aren’t what I wanted...*

*...it must be the gage’s fault!”*



# The Implications

- Measurement results have some inherent uncertainty.
  - The measured result is only an estimate of the “true” or “correct” value.
- Uncertainty:

“How far from the truth can my result be.”



# Measurement Uncertainty

- Traditionally, we dealt with “*accuracy*” and “*repeatability*”.
  - Accuracy:  
*Are we targeted?*
  - Repeatability:  
*Do we get the same value again & again*
- “*Uncertainty*” encompasses these ideas in a more comprehensive manner.



# Measurement Uncertainty

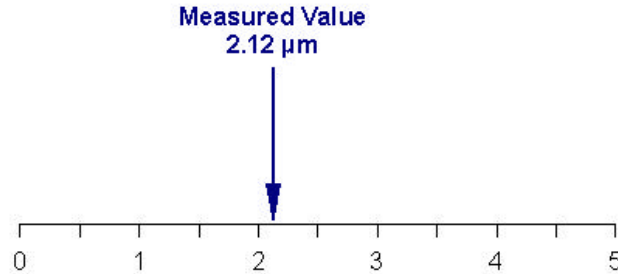
- Many are intimidated by the concept of uncertainty...

*... it's not that difficult.*

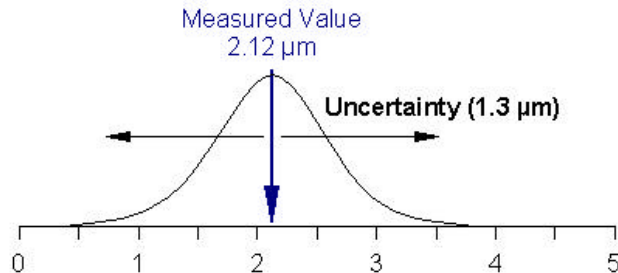
- Measurement uncertainty is trying to predict where the true value is given my measured value.
  - It relates the “measurement” to the true value of the “measurand”.

# Measurement Uncertainty

- Given my result:



- Where might the true value lie? ( $2.12 \pm 1.3$ )

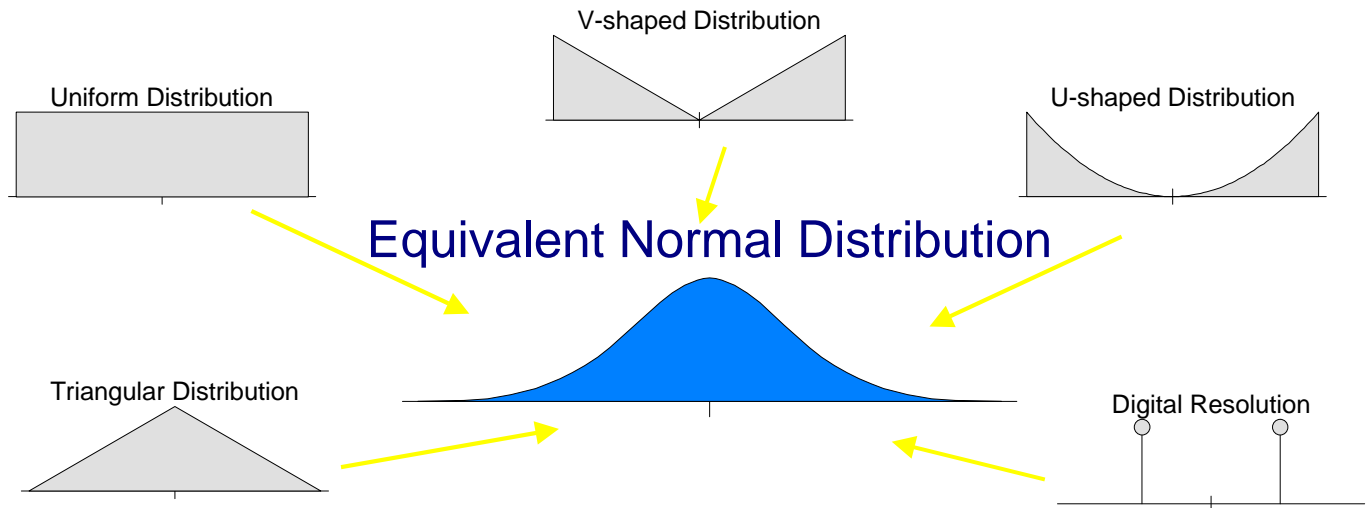


# Measurement Uncertainty

- Consider the Contributors (FMEA-style)
  - What are the elements of the measurement system that can make it be wrong?
  - Determine how each can affect the result and express it as a standard deviation.
  - Combine the standard deviations to get the distribution.
    - Uncertainty is typically expressed as  $\pm 2$  standard deviations of this distribution.

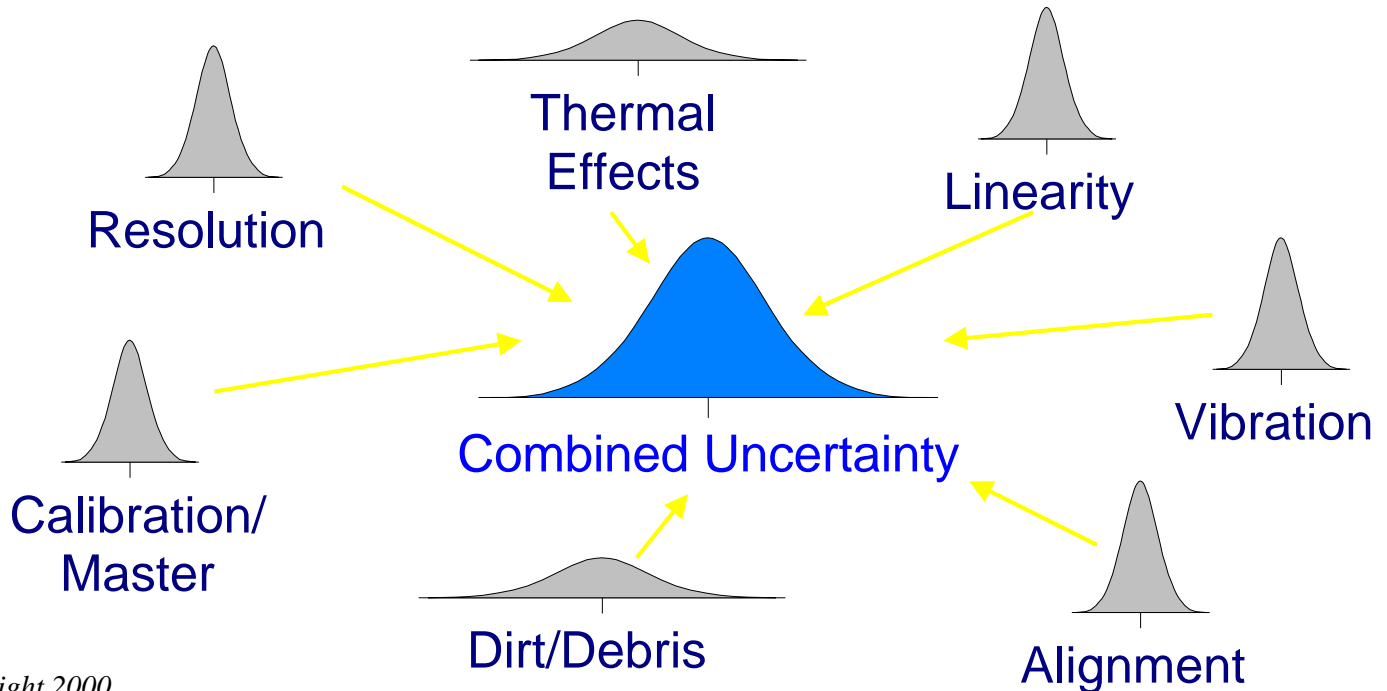
# Measurement Uncertainty

- Each contributor can be approximated as normal distribution of errors
  - Even if the errors themselves are normally distributed.



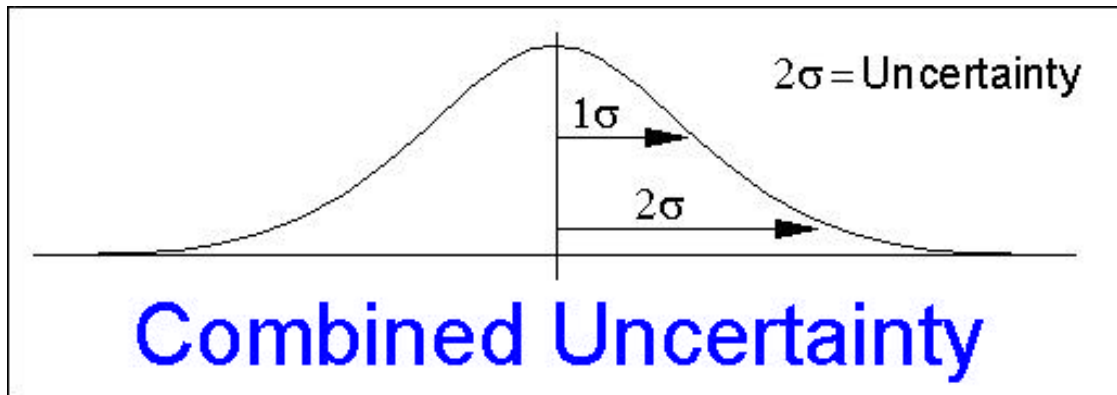
# Measurement Uncertainty

- Once you have a distribution for all contributors you simply “pool” them.



# Measurement Uncertainty

- Measurement Uncertainty is typically expressed as a “*2 Standard Deviation*” value.
  - The “2” is the “coverage factor”
    - (95% confidence)

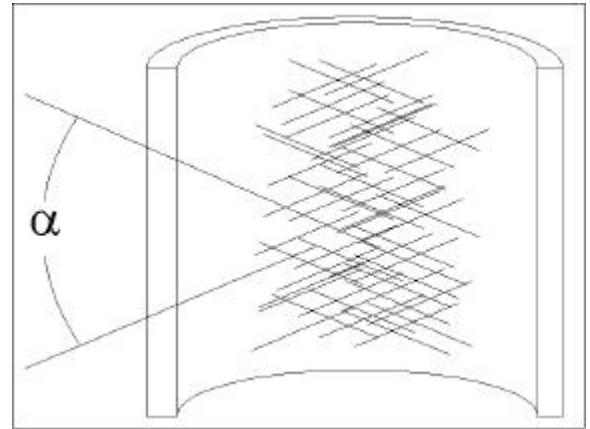


# The Implications (continued)

- When a measured result is reported, there must be an associated uncertainty. This dictates the action.
- Applications:
  - Determining *when* to adjust the process
  - Pre-shipment or Receiving inspection
  - Customer/Supplier Disputes
  - Correlation problems

# Example: Cross-hatch Angle

- The Goal:
  - Does the cross-hatch angle meet the specification ( $45^\circ \pm 5^\circ$ )? Should the process be adjusted?
- The measurand
  - The included angle based on the predominant valleys as shown in the Figure.





# Example: Cross-hatch Angle

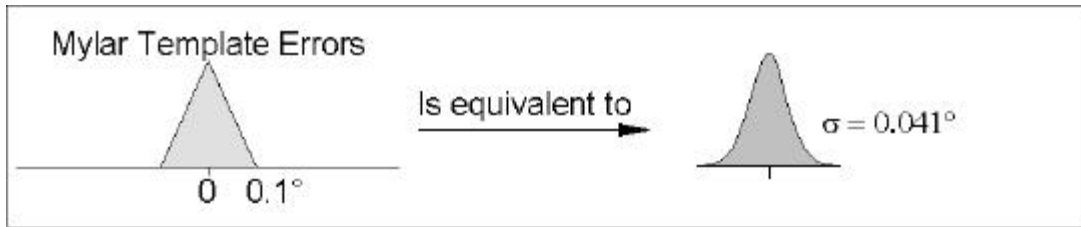
- The Measurement
  - Method selection:
    - Mylar Template; visual assessment
  - Measured value was  $47.5^\circ$
- The implications.
  - Need to know the uncertainty before acting on the result.

# Example: Cross-hatch Angle

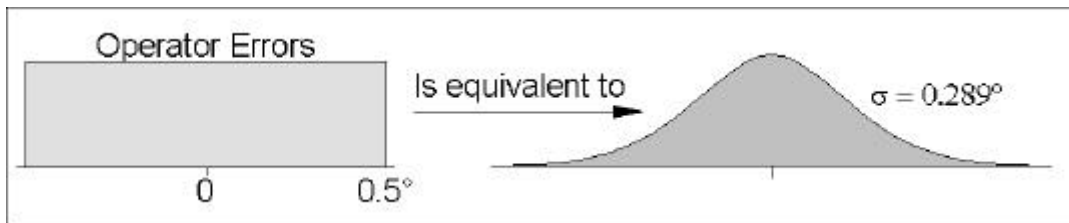
- The implications (continued)
  - Estimate the uncertainty
- Primary Contributors:
  - Printed Mylar Template:
    - Printing good to within 0.1 degrees
    - Assume triangular distribution
  - Manual Interpretation
    - Operator, lighting, etc. good to within 0.5 degrees
    - Assume uniform distribution

# Example: Cross-hatch Angle

- Uncertainty Estimation
  - Mylar Template:



- Operator



# Example: Cross-hatch Angle

Combining the contributions

$$S_{combined} = \sqrt{S_{mylar}^2 + S_{operator}^2}$$

$$S_{combined} = \sqrt{0.041^2 + 0.289^2} = 0.292^\circ$$

Expanding the uncertainty

$$U_{95} = k \cdot S_{combined} = 2 \cdot 0.292 = 0.584^\circ$$

# Example: Crosshatch Angle

- The measured cross-hatch angle is:

$$\underline{47.5^\circ \pm 0.6^\circ}$$

- Given our estimated uncertainty the true value should lie between

$$46.9^\circ - 48.1^\circ$$

- Reminder: The spec is  $45.0^\circ \pm 5^\circ$

# Summary

- Metrology is a tool for understanding.
  - A tool is only effective if it is applied properly.
- Understand the elements of measurement
  - Goal (Question)
  - Measurand (Result to be Determined)
  - Measurement (The Process)
  - Implications (Uncertainty)